

**Gino TIRONI**

**Sequential order of compact sequential spaces**

*Abstract.* The problem of finding compact sequential spaces of arbitrary order is presented and its dependence on the assumptions of the Theory of Sets is examined. Arhangel'skiĭ and Franklin [AF] found examples of sequential spaces (but not compact) of any order in ZF. Baškirov [B] proved, under CH, that there are compact Hausdorff spaces of any sequential order up to and including  $\omega_1$ . The results of Baškirov, concisely presented in a Doklady article, are completely revisited and compared with the results of Dow [D1, D2] under MA.

A short comparison is made also with results of Kannan on the same subject, under CH.

If  $K_\alpha$  and  $K_\beta$  are Baškirov spaces of sequential order  $\alpha$  and  $\beta$  respectively, then  $K_\alpha \times K_\beta$  has sequential order  $\max(\alpha, \beta)$ .

**References**

- [AF] A. V. Arhangel'skiĭ and S. P. Franklin, New ordinal invariants for topological spaces, Michigan Math. Jour. **15** (1968) 313-320
- [B] A. I. Baškirov, The classification of quotient maps and sequential bcompacta, Soviet Math. Dokl. **15** (1974) 1104-1109.
- [D1] Alan Dow, On MAD families and sequential order.  
See <http://www.math.uncc.edu/~adow/Others.html> under the title "On the sequential order of Compact spaces".
- [D2] Alan Dow, Sequential order under MA, Topology Appl. **146-147**(2005) 501-510.
- [K] V. Kannan, Ordinal invariants in topology II. Sequential order of compactifications, Compositio Mathematica, **39**, 2 (1979) 247-262.